# Dynamic Performance Characteristics

Meteorology 432 Spring 2013

## Changing modes

 When the input to a sensor is <u>changing rapidly</u>, we observe performance characteristics that are due to the changing input and <u>not related</u> to <u>static performance</u>.

- Redefine "linear"
  - Static: constant static sensitivity.
  - Dynamic: applicability of the superposition property.
- A sensor can be <u>nonlinear</u> in the static sense, but could be <u>linear</u> in the dynamic sense (modeled by a linear differential equation).

### **Dynamic Performance Characteristics**

 Define the way instruments react to measured quantity fluctuations.

Examples

## First Order Systems

- Differential equations describe the behavior of physical systems.
- First property: For a <u>linear</u> system, the response to a sum of inputs is simply the sum of the responses to those inputs!
  - "The response to a sum is the sum of the responses".
  - Superposition principle.
- Second property: For a <u>linear</u> system, the response to an input multiplied by a constant is the response to the input applied separately multiplied by the same constant.
  - "If the input is multiplied by a constant, the output is multiplied by the same constant."

#### **Definitions**

- Static State: systems variables do not depend on time.
  - All time derivatives in the differential equation are equal to zero.
- Dynamic State: equations contain time derivatives.
- When forces are applied at <u>discrete points</u> and are transmitted by <u>discrete components</u> within the system, the system can be defined by <u>lumped parameters</u>.
- Dynamic performance analysis is concerned with modeling the performance of <u>dynamic</u>, <u>lumped parameter systems</u>, with <u>ordinary</u> <u>differential equations</u>, where <u>time</u> is the independent variable.
  - If it is necessary to describe the variation across space, the system must be described with <u>distributed parameters</u> (<u>continuum</u>), and is modeled by <u>partial differential equations</u>.
- Order of the system = number of dynamic performance parameters.

## Ramp Input - Example

- Suppose you have subjected your thermometer to a steadily rising temperature after it was kept at a constant temperature for a while (equilibrium with environment).
- The reading of the thermometer will always lag with respect to the real temperature – it takes time to settle.

 To minimize this effect, you would choose a thermometer with a very small time constant.

# Sinusoidal Input – Example

- Suppose our thermometer was kept at equilibrium with the environment, and then was subjected to a sinusoidal input (change in temperature)
- If the temperature variation is slow (low frequency), the sensor output will simply follow the ambient input.
- If the temperature variation is very fast, the sensor output will be very small (it will stay at the reading prior to the beginning of the input)
  - Simply unable to follow the fast variations!!
- What is slow and what is fast?
  - It relates to the natural "scale" or the time constant or the frequency.

# Experimental Determination of Dynamic Performance Parameters

- Determine the time constant:
  - Apply step-function input.
  - Determine the time to reach 63% of the steady state value.
- This approach is practical only under ideal conditions.
  - If the data is noisy or if the data are missing in this critical time period, the method fails.
- What do we do?
  - Better to apply other methods
  - Linear regression method